

CHAPTER 5		CHAPTER 7		CHAPTER 10	
Methods of Collecting Data		Discrete Random Variables (Ch7) vs. Continuous Random Variables (Ch8)		Definitions	
NOTE: Both methods involve observations, but...		Random variable A function or rule that assigns a number to each outcome of an experiment.		Point Estimator:	A <b>single value</b> that estimates an unknown <i>population parameter</i> .
Observational	An observational study finds the relationship between changes that already exist. <ul style="list-style-type: none"><li>Easier to perform</li><li>More difficult to draw cause/effect conclusions from</li></ul>	Discrete random variable Values are countable, e.g. number of courses, number of siblings, age (in years).		Interval Estimator:	A <b>range of values</b> that estimate and unknown <i>population parameter</i> .
		Continuous random variable Values are uncountable - typically measured quantities, e.g. height, weight, time, speed		Qualities of a Good Estimator	
Experimental	An experiment requires you to observe what happens when you make some sort of change. <ul style="list-style-type: none"><li>Can be unethical</li><li>Subjects randomly assigned to groups</li><li>Possible to draw cause/effect conclusions</li></ul>	Discrete Probability Distributions		Unbiased:	The average (expected) value of the estimator equals the population parameter being estimated.
		Binomial Distribution		Consistency:	The estimator gets closer to the population parameter as the sample size increases.
Types of Samples		Is it a Binomial Experiment?		Relative Efficiency:	If two unbiased estimators are available as estimators, choose the one with less variability.
Simple Random Sample	A sample selected in such a way that every possible sample with the same number of observations is equally likely to be chosen.	Probability A table, formula, or graph that describes the values of a random variable and the probability associated with these values		Interpreting a Confidence Interval	
		Requirements for a Distribution of a Discrete Random Variable...		"The mean is estimated to fall between (LCL*) and (UCL*). This type of estimation is correct (confidence level*)% of the time."	
Stratified Random Sample	Obtained by separating the population into mutually exclusive sets, or strata, and then drawing simple random samples from each stratum.	Expected Value of X (non-binomial) $E(X) = \mu = \sum_{all\ x} xP(x)$		*Fill in the values	
		Variance of X (non-binomial) $V(x) = \sigma^2 = \sum_{all\ x} (x - \mu)^2 P(x)$		Confidence Interval Estimator of $\mu$	
Cluster Sampling	A simple random sample of groups or clusters of elements.	Standard Deviation of X (non-binomial) $\sigma = \sqrt{\sigma^2}$		Lower Confidence Limit (LCL):	$\bar{x} - z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$
		Example (Non-binomial)		Upper Confidence Limit (UCL):	$\bar{x} + z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$
Sampling vs Non-Sampling Error	Difference between what a sample predicts and the true population paramter. Occurs because a sample is being used to make inferences about an entire population.	Question: Two balls are selected randomly without replacement from a jar containing 4 red balls and 6 black balls. Let X be the number of red balls selected.		Sample Size (given the bound on error of estimation B): $n = \left(\frac{z_{\alpha/2}\sigma}{B}\right)^2$	
		a) Give the probability distribution of x		Common Confidence Levels and $z_{\alpha/2}$	
Sampling Error		b) Find the expected value and variance of x		Factors Affecting WIDTH of Confidence Intervals	
		Laws of Expected Value Laws of Variance		As sample size n ↑ ... width ↓ (GOOD!!!)	
Non-Sampling Error	Errors resulting from mistakes made when collecting data. <ul style="list-style-type: none"><li>Responses being recorded incorrectly</li><li>Some participants not responding</li><li>Biased sample</li></ul>	Normal Distribution Probabilities Ch.8 (x) example		As sample size n ↓ ... width ↑ (wide intervals are BAD)	
		Ch.9 (x̄) example		As confidence level (1-α) ↑ ... width ↑ (wide intervals are BAD)	
STATS DOESN'T SUCK		REVERSE Ch.8 (Given a probability and asked to find boundary)		As confidence level (1-α) ↓ ... width ↓ (loss of confidence is BAD)	
CHAPTER 8		Ch.9 (p̂) example		As variance ↑ ... width ↑ (BAD: can't adjust variance)	
Probability Density Functions		REVERSE STEPS 2+3		As variance ↓ ... width ↓ (BAD: can't adjust variance)	
Continuous Random Variable		Convert z to x, x̄, or p̂		As sample mean ↑ ... width is unaffected	
Probability Density Function		x = zσ + μ ...Ch. 8		As sample mean ↓ ... width is unaffected	
Requirements: (range is a ≤ x ≤ b)		x̄ = zσ_x + μ ...Ch.9 (x̄)		Sampling Distribution of X̄	
1. f(x) ≥ 0 for all x between a and b		p̂ = zσ_p + p ...Ch.9 (p̂)		... shows the probabilities for all possible sample means for a given sample size (n).	
2. The total area under the curve between a and b is 1.0		x = zσ + μ		Mean Standard Error	
Uniform Density Function		x = (1.28)(4) + 20		μ_x̄ = μ σ_x̄ = $\frac{\sigma}{\sqrt{n}}$ (standard deviation of the sampling distribution)	
f(x)		x = 25.12		Central Limit Theorem:	
P(x1 < X < x2) = Base × Height		x = 25.12 separates the top 10% from the bottom 90%		If X is normal, then X̄ is normal. If X is nonnormal, then X̄ is approx normal for sufficiently large sample sizes.	
= (x1 - x2) × $\frac{1}{b-a}$				Convert X̄ to a z-score: $z = \frac{\bar{x} - \mu}{\sigma_{\bar{x}}}$	
				Sampling Distribution of X̄1-X̄2	
				$z = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$	
				Sampling Distribution of p̂	
				p̂ is approx normally distributed provided that np and n(1 - p) are greater than or equal to 5.	
				Expected p̂ Standard Error of p̂	
				E(p̂) = p σ_p̂ = $\sqrt{\frac{p(1-p)}{n}}$	
				Convert p̂ to a z-score: $z = \frac{\hat{p} - p}{\sqrt{p(1-p)/n}}$ p̂ = $\frac{X}{n}$	